

Quiz #08 – MATH 2421

Fall 2007

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Name : \_\_\_\_\_

Directions: No calculators, books, or notes. Show algebra. Be sure to highlight your final answer!  
 $r^2 = x^2 + y^2$ ,  $x = r \cos(\theta)$ ,  $y = r \sin(\theta)$ .

1. [4 pts.] The surface area differential is

$$dS = \sqrt{1 + (f_x)^2 + (f_y)^2} dA.$$

Suppose we have the upper cone  $z = 2\sqrt{x^2 + y^2}$ . Find the surface area above the region in the xy-plane  $R$ :  $x^2 + y^2 \leq 4$ .

$r \, dr \, d\theta$

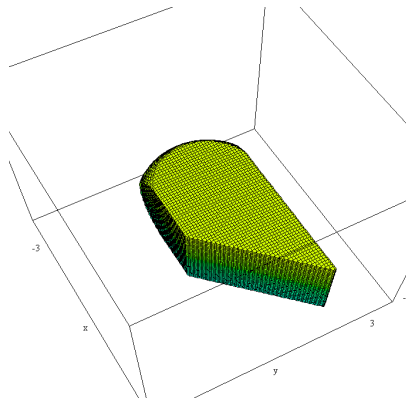
$r$ :

$\theta$ :

2. [3 pts.] We have a solid  $Q$  bounded by the plane  $x = y + 2$  and the hemisphere  $x = -\sqrt{2 - y^2 - z^2}$ .

The solid is also bounded by the planes  $y = -1$ ,  $y = 1$ ,  $z = -1$ , and  $z = 1$ .

Suppose the density function is  $\sigma(x, y, z) = x^2 + 2z^2$ .



There is only ONE reasonable choice for the variable of integration in the INNER integral.

Set up but DO NOT EVALUATE the TRIPLE INTEGRAL which represents the mass:

$$m = \iiint_Q \sigma(x, y, z) \, dV$$

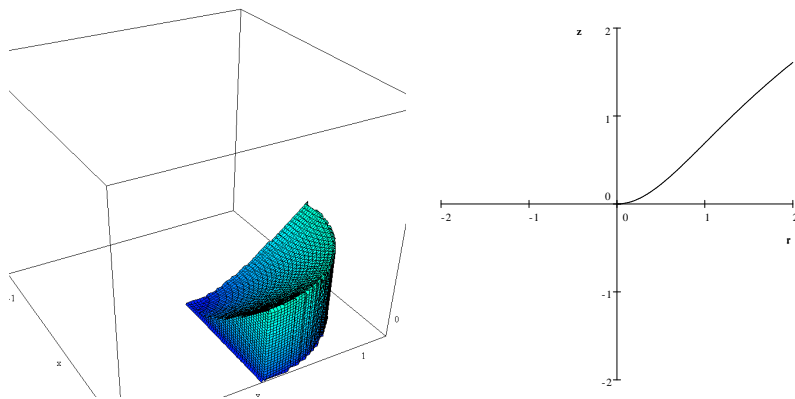
3. [3 pts.] Suppose we have the surface of revolution

$$z = \ln(1 + x^2 + y^2) = \ln(???) .$$

Hint: This is easy to transform into cylindrical coordinates. [The  $rz$ -plane generating curve is given below as an added hint.]

The solid  $Q$  traps the volume *beneath* this surface, above the circular region  $x^2 + y^2 \leq 1$  ONLY IN QUADRANT I.

The density function is  $\sigma(x, y, z) = x + y$ .



Set up but DO NOT EVALUATE the CYLINDRICAL COORDINATES TRIPLE INTEGRAL which represents the mass.

$dz r dr d\theta$

$z$ :

$r$ :

$\theta$ :