

# Laplace Transform Table

(Adapted from Table 5.1 of Kohler and Johnson)

Time Domain Function $f(t)$ , $t \geq 0$	Laplace Transform $F(s)$
$a$	$\frac{a}{s} \quad s > 0$
$h(t) = \begin{cases} 1, & t \geq 0 \\ 0, & t < 0 \end{cases}$	$\frac{1}{s} \quad s > 0$
$t^n, \quad n = 1, 2, 3, \dots$	$\frac{n!}{s^{n+1}}, \quad s > 0$
$e^{\alpha t}$	$\frac{1}{s - \alpha}, \quad s > \alpha$
$\sin(\omega t)$	$\frac{\omega}{s^2 + \omega^2}, \quad s > 0$
$\cos(\omega t)$	$\frac{s}{s^2 + \omega^2}, \quad s > 0$
$\sinh(\alpha t)$	$\frac{\alpha}{s^2 - \alpha^2}, \quad s >  \alpha $
$\cosh(\alpha t)$	$\frac{s}{s^2 - \alpha^2}, \quad s >  \alpha $
$e^{\alpha t} f(t)$ , with $ f(t)  \leq M e^{\alpha t}$	$F(s - \alpha), \quad s > \alpha + a$
$e^{\alpha t} h(t)$	$\frac{1}{s - \alpha}, \quad s > \alpha$
$e^{\alpha t} t^n, \quad n = 1, 2, 3, \dots$	$\frac{n!}{(s - \alpha)^{n+1}}, \quad s > \alpha$
$e^{\alpha t} \sin(\omega t)$	$\frac{\omega}{(s - \alpha)^2 + \omega^2}, \quad s > \alpha$
$e^{\alpha t} \cos(\omega t)$	$\frac{(s - \alpha)}{(s - \alpha)^2 + \omega^2}, \quad s > \alpha$

Time Domain Function $f(t)$ , $t \geq 0$	Laplace Transform $F(s)$
$f(t - \alpha)h(t - \alpha)$ , $\alpha \geq 0$ with $ f(t)  \leq Me^{at}$	$e^{-\alpha s}F(s)$ , $s > a$
$h(t - \alpha)$ , $\alpha \geq 0$	$\frac{e^{-\alpha s}}{s}$ , $s > 0$
$f'(t)$ , with $f(t)$ continuous and $ f'(t)  \leq Me^{at}$	$sF(s) - f(0)$ , $s > \max\{a, 0\}$
$f''(t)$ , with $f'(t)$ continuous and $ f''(t)  \leq Me^{at}$	$s^2F(s) - sf(0) - f'(0)$ , $s > \max\{a, 0\}$
$\int_0^t f(u) du$ , with $ f(t)  \leq Me^{at}$	$\frac{F(s)}{s}$ , $s > \max\{a, 0\}$
$\frac{1}{2\omega^3}(\sin \omega t - \omega t \cos \omega t)$	$\frac{1}{(s^2 + \omega^2)^2}$ , $s > 0$
$\frac{t}{2\omega} \sin \omega t$	$\frac{s}{(s^2 + \omega^2)^2}$ , $s > 0$
$tf(t)$	$-F'(s)$